(10 pts) 1. State the sampling theorem. (You may use your own words but

be precise!)

The sampling theorem states that

a signal can be completely recovered from it's sampling

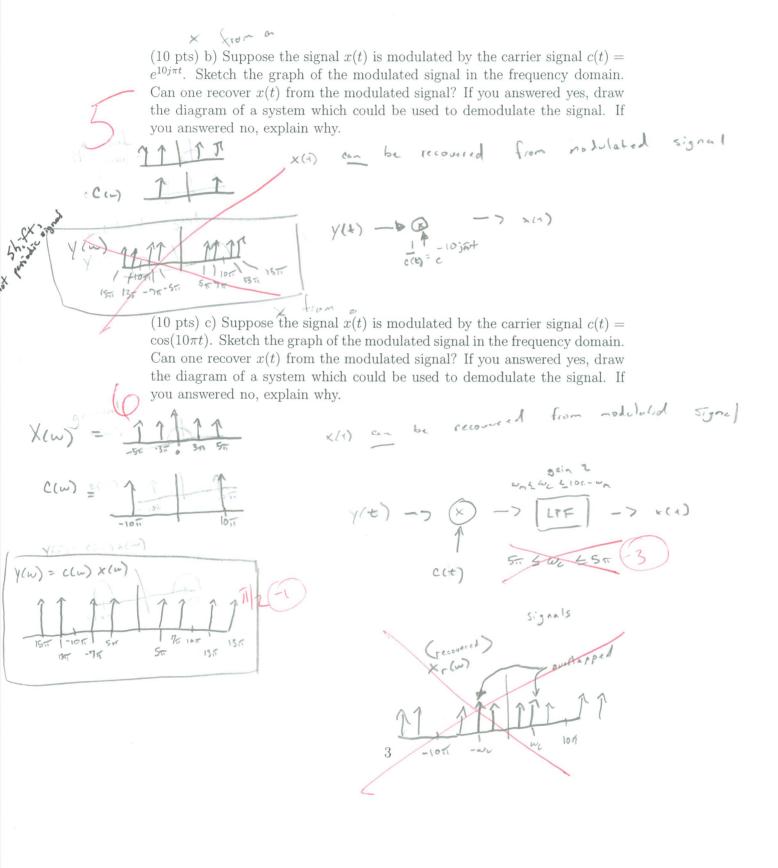
as long as the frequency it was sampled at exceeds the Nyquist rate (2 mm)

what is Wm2

signal must be band lined | XIw) =0 (4) > wn

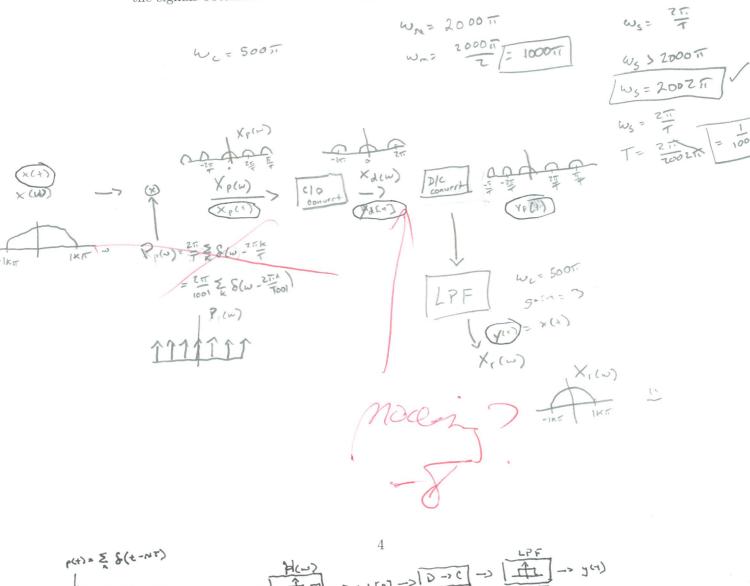
2. Consider the signal  $x(t) = \cos(3\pi t) + \cos(5\pi t)$ . (5 pts) a) Is x(t) band-limited? If so, what is the Nyquist rate for this signal (Justify your answers.)

X(w) = 1 1 1 1 res, x(+) is band limited Wm = 5 TT W = 2 wm = 2 (57) 1 WN = 10TT



2

(20 pts) 3. DT processing of CT signals. A CT signal x(t) with Nyquist rate equal to  $2000\pi$  is the input of a CT system consisting of a low-pass filter with gain 3 and cut-off frequency  $500\pi$ . Draw the diagram of an equivalent system which would sample x(t), process the samples using a DT system, and reconstruct a CT signal from the processed samples. (Don't forget to specify an appropriate frequency for the sampling as well as the frequency response of the DT system.) Illustrate all the steps of the system by sketching (in the frequency domain) the graph of an input signal together with the graphs of the signals obtained at each of the intermediate steps of the system.



(15 pts) 4. Compute the Laplace transform of the following signal without using the table of Laplace transform pairs:

$$x(t) = e^{-2t}u(t) + e^{5t}u(-t).$$

$$x(s) = \int_{-\infty}^{\infty} x(4) e^{-st} dt$$

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$$x(s) = \int_{-\infty}^{\infty} e^{-$$