

ECE 301 Quiz 3.

7/14 (Tue)

$x(t) = t e^{-2t} \sin(4t) u(t)$
Determine its Fourier Transform.

Quiz 3

7/14

$$x(t) = t e^{-2t} \sin(4t) u(t)$$

Determine its FT.

(ANSWER)

$$e^{-2t} u(t) \xleftrightarrow{\mathcal{F}} \frac{1}{2 + j\omega}$$

$$e^{-2t} u(t) \sin(4t) \xleftrightarrow{\mathcal{F}} \frac{1}{2j} \frac{1}{2 + j(\omega - 4)} - \frac{1}{2j} \frac{1}{2 + j(\omega + 4)}$$

$$t (e^{-2t} u(t) \sin(4t)) \xleftrightarrow{\mathcal{F}} j \frac{d}{d\omega} \left\{ \frac{1}{2j} \frac{1}{2 + j(\omega - 4)} - \frac{1}{2j} \frac{1}{2 + j(\omega + 4)} \right\}$$
$$= \frac{1}{2} \frac{-j}{(2 + j(\omega - 4))^2} + \frac{1}{2} \frac{-j}{(2 + j(\omega + 4))^2}$$