1. Let $p_{i, j}, p_{n}$, and $p$ be real numbers for all $i, j, n$. Suppose

$$
\begin{aligned}
& p_{1, j} \rightarrow p_{1} \\
& p_{2, j} \rightarrow p_{2}
\end{aligned}
$$

... and in general

$$
p_{i, j} \rightarrow p_{i}
$$

as $j \rightarrow \infty$. Further assume

$$
p_{n} \rightarrow p
$$

Prove or disprove that $\left\{p_{j, j}\right\}$ converges.
2. Let $a_{i, j}, a_{n}$, and $a$ be positive real numbers for all $i, j, n$. Suppose

$$
\begin{aligned}
& \sum_{j=1}^{\infty} a_{1, j}=a_{1} \\
& \sum_{j=1}^{\infty} a_{2, j}=a_{2}
\end{aligned}
$$

and in general

$$
\sum_{j=1}^{\infty} a_{i, j}=a_{i}
$$

Further assume

$$
\sum_{j=1}^{\infty} a_{j}=a
$$

Prove or disprove

$$
\sum_{j=1}^{\infty} a_{j, j}
$$

converges.

